## **Short-Range Order and Charge Transport in SiO***x***: Experiment and Numerical Simulation**

**V.** A. Gritsenko<sup>*a*, *b*, *c*<sub>\*</sub>, **Yu.** N. Novikov<sup>*a*</sup>, and A. Chin<sup>*d*</sup></sup>

*a Rzhanov Institute of Semiconductor Physics, Siberian Branch, Russian Academy of Sciences, Novosibirsk, 630090 Russia b Novosibirsk State University, Novosibirsk, 630090 Russia*

*c Novosibirsk State Technical University, Novosibirsk, 630090 Russia*

*d National Chiao Tung University, Hsinchu, Taiwan, Republic of China*

*\*e-mail: grits@isp.nsc.ru*

Received March 1, 2018

**Abstract**—The structure of nonstoichiometric silicon oxide (SiO*x*) has been studied by the methods of highresolution X-ray photoelectron spectroscopy and fundamental optical-absorption spectroscopy. The conductivity of  $SiO<sub>x</sub>$  ( $x = 1.4$  and 1.6) films has been measured in a wide range of electric fields and temperatures. Experimental data are described in terms of the proposed SiO*x* structure model based on the concept of fluctuating chemical composition leading to nanoscale fluctuations in the electric potential. The maximum amplitude of potential fluctuations amounts to 2.6 eV for electrons and 3.8 eV for holes. In the framework of this model, the observed conductivity of SiO*x* is described by the Shklovskii–Efros theory of percolation in inhomogeneous media. The characteristic spatial scale of potential fluctuations in SiO*x* films is about 3 nm. The electron-percolation energy in  $SiO<sub>1.4</sub>$  and  $SiO<sub>1.6</sub>$  films is estimated to be 0.5 and 0.8 eV, respectively.

**DOI:** 10.1134/S1063785018060196

Amorphous nonstoichiometric silicon oxide (a-SiO*x*) is a key dielectric in modern microelectronics. By varying the chemical composition of  $SiO<sub>x</sub>$ , it is possible to change its optical and electrical properties, including photoluminescence (PL) [1], within broad limits. The optical spectra of  $SiO<sub>x</sub>$  films depend to a considerable degree on the presence of embedded silicon nanoclusters, and the optical properties of these films are determined by the concentration and size of Si-nanoclusters [2]. Passivating SiO*x* layers are used in poly-Si contacts of solar cells [3], nonvolatile memory based on localized charge storage [4], and resistive memory devices [5].

The present work was aimed at an experimental investigation of the short-range order in SiO*x* films by means of high-resolution X-ray photoelectron spectroscopy (HRXPS), measurement of their fundamental optical-absorption spectra, elucidation of the mechanism of charge transport, and estimation of the characteristic spatial size and amplitude of potential fluctuations in terms of the Shklovskii–Efros percolation theory.

Samples of about 100-nm-thick a-SiO*x* layers were synthesized by the method of chemical-vapor deposition method based on the interaction of  $SiH<sub>4</sub>$  and N<sub>2</sub>O vapors at  $640^{\circ}$ C. The SiO<sub>x</sub>-layer composition could be changed by varying the  $SiH_4/N_2O$  flux ratio. The films were deposited onto [100]-oriented *n*-type silicon substrates with a resistivity of ~10  $\Omega$  cm. The HRXPS spectra of  $SiO<sub>1.4</sub>$  films were measured using a Kratos AXIS-HS system with a source of monochromated  $\Delta I K_\alpha$  radiation. The spectra of optical absorption in the visible and near-IR frequency range were recorded on Shimadzu UV-300 and Specord S-300 UV-Vis spectrophotometers. Current–voltage (*I*–*V*) characteristics were measured using  $SiO<sub>x</sub>$  film samples with deposited aluminum contacts of  $5 \times 10^{-3}$  cm<sup>2</sup> area.

In the literature, the structures of nonstoichiometric compounds are usually described in terms of the random-bonding (RB) or random-mixture (RM) models [6]. The RB model assumes that SiO*x* consists of  $SiO_vSi_{4-v}$  tetrahedra of five kinds ( $v = 0, 1, 2, 3$ , and 4) and probability  $W_{\rm v}^{\rm RB}$  of finding a v-th-type tetrahedron (i.e., the fraction of these tetrahedra) in SiO*<sup>x</sup>* with composition  $x$  is defined as [6]

$$
W_{\mathbf{v}}^{\text{RB}}(x) = \frac{4!}{\mathbf{v}!(4-\mathbf{v})!} \left(\frac{x}{2}\right)^{\mathbf{v}} \left(1 - \frac{x}{2}\right)^{4-\mathbf{v}}.\tag{1}
$$

According to the RM model,  $SiO_x$  consists of two phases: amorphous silicon (a-Si) and  $SiO<sub>2</sub>$  (i.e., of  $SiSi<sub>4</sub>$  and  $SiO<sub>4</sub>$  tetrahedra, respectively), the fractions of which are determined as  $W_0^{RM}(x) = 1 - x/2$  and  $W_4^{RB}(x) = x/2$ , respectively.



**Fig. 1.** (a) Experimental photoelectron spectra of Si 2*p* levels in  $SiO<sub>1.4</sub>$  (solid curves) and results of numerical simulation using RB, RM, and IM models (dashed curves); (b) spectral dependences of light absorption in SiO*x* films with  $x = 0$ , 1.4, 1.6, and 2 (SiO<sub>2</sub> spectrum reproduced from [7]).

The photoelectron energy spectrum *I*(*E*) is described using  $W_{\rm v}$  peaks defined in the RB and RM models broadened with Gaussian function by the following formula:

$$
I(E) = \sum_{v} W_{v} e^{(E - E_{v})^{2} / (2\sigma_{v}^{2})},
$$
 (2)

where  $E_v$  and  $\sigma_v$  are the peak energy and half-width, respectively, for tetrahedra of the νth type.

Figure 1a shows the experimental photoelectron spectra of Si  $2p$  levels in SiO<sub>x</sub> (solid curves). The peak of  $Si^{4+}$  with binding energy  $E_0 = 103.5$  eV and halfwidth  $\sigma_0 = 1.2$  eV refers to the a-SiO<sub>2</sub> phase; the peak of Si with binding energy  $E_4$  = 99.5 eV, and half-width  $\sigma_4$  = 0.6 eV refers to the a-Si phase, while the binding energies and half-widths of the peaks for  $Si^{3+}$ ,  $Si^{2+}$ , and  $Si<sup>+</sup>$  are determined by linear interpolation of  $E<sub>0</sub>$ ,

 $E_4$ ,  $\sigma_0$ , and  $\sigma_4$  values with the corresponding numbers of oxygen atoms.

The top panel in Fig. 1a compares the experimental spectrum (solid curve) of Si 2*p* levels to the results of numerical simulation using the RB model (dashed curve). The latter Si 2*p* spectrum has a single peak with a binding energy of 102.5 eV. The maximum contribution to the calculated spectrum is due to SiO*x*, while the contributions from  $SiO<sub>2</sub>$  and Si are underestimated. Calculation of the Si 2*p* spectrum using the RM model (Fig. 1a, middle panel) predicts the existence of two peaks corresponding to  $SiO<sub>2</sub>$  and Si phases. This calculation overestimates the contribution due to Si phase and underestimates the contribution of  $SiO_x$  phase. Thus, neither the RM nor RB model adequately describes the experimental photoelectron spectrum.

To describe the experimental HRXPS data, we propose to use an intermediate model (IM), according to which  $SiO<sub>x</sub>$  consists of tetrahedra of five kinds (similarly to the RB model), but the distribution of these tetrahedral differs from that given by formula (1) for the RB model. In the proposed IM model, fractions  $W_v$  of  $SiO_vSi_{4-v}$  tetrahedra of five kinds ( $v =$ 0, 1, 2, 3, and 4) are selected so as to ensure the best fit of the experimental spectrum to the *I*(*E*) spectrum calculated by the Newton method using formula (2). Proper selection of the contributions of various types of tetrahedral provided good coincidence of the result of calculations to experiment (Fig. 1a, bottom panel).

For determining the bandgap width of SiO*x* films, we have measured the spectra of fundamental optical absorption. Figure 1b presents spectral dependences of the optical absorption edge for a-Si, a-SiO*x*, and  $SiO<sub>2</sub>$  films (the spectrum of  $SiO<sub>2</sub>$  was taken from [7]). The absorption edge of  $SiO_x$  varies within 3.1–3.4 eV.

Comparison of the simulated photoelectron spectra and data on the optical absorption indicates that the obtained films contain phases of stoichiometric  $SiO<sub>2</sub>$ , nonstoichiometric silicon suboxides  $SiO<sub>v</sub>$ , and amorphous silicon (Fig. 1). Silicon suboxides SiO*<sup>y</sup>* consist of  $SiSiO<sub>3</sub>$ ,  $SiSi<sub>2</sub>O<sub>2</sub>$ , and  $SiSi<sub>3</sub>O$  tetrahedra, the presence of which is confirmed by the results of HRXPS measurements for  $SiO<sub>1.4</sub>$  films.

Figure 2 shows schematic two-dimensional (2D) energy diagrams of the (a)  $SiO_x$  structure and (b) potential fluctuations (according to the Shklovskii– Efros percolation theory) in heavily doped compensated semiconductor. The horizontal line *A*–*A* (Fig. 2a) indicates to what the energy diagram refers, the line  $E = 0$  indicates the zero electron energy (vacuum energy level),  $E<sub>e</sub>$  is the bandgap width of a-Si,  $E<sub>c</sub>$  is the conduction-band bottom, and  $E<sub>v</sub>$  is the valence-band top. Since  $E_g = 1.6$  eV in a-Si, the minimum bandgap width in  $SiO_x$  also amounts to 1.6 eV. Increase in the bandgap width corresponds to growing content of sili-



**Fig. 2.** (a) Schematic 2D diagram of SiO*x* structure and the energy diagram in *A*–*A* cross section; (b) potential fluctuations (according to the Shklovskii–Efros percolation theory) in heavily doped compensated semiconductor (μ is the Fermi level).

con suboxides. The maximum bandgap width in SiO*<sup>x</sup>* is the same as that in  $SiO<sub>2</sub>$  (i.e., 8.0 eV). Taking into account that the electron affinity in a-Si is 3.6 eV and that in  $SiO<sub>2</sub>$  is 1 eV, and using the diagram in Fig. 2a, the maximum amplitude of potential fluctuations in SiO*x* can be estimated as 2.6 eV for electrons and 3.8 eV for holes.

Figure 3 shows the experimental current–voltage characteristics (points) of  $SiO<sub>1.4</sub>$  and  $SiO<sub>1.6</sub>$  films in comparison to the results of calculations (solid lines) based on the Shklovskii–Efros percolation model [8]. This model has been previously used for the description of charge transport in nonstoichiometric HfO*<sup>x</sup>* films [9]. In the present work, it is assumed that the random potential modulating the bandgap width has rather large amplitude. In this case, the quantum effects can be ignored and the boundary of delocalized states coincides with the percolation level [8]. The electric conductance in this system is determined by electrons thermoactivated to the delocalized states (for the sake of simplicity, the transport of holes is not considered). Then, according to theory [8], the current– voltage characteristics of disordered materials are described by the following expression:

$$
J = J_0 \exp\left(-\frac{W_p^e - (CeaV_0^{(1-\gamma)/\gamma}F)^{\gamma}}{kT}\right),\tag{3}
$$

where  $J_0$  is the preexponential factor,  $W_p^e$  is the percolation energy for electrons,  $C = 0.25$  is a constant coefficient,  $\gamma = 0.52$  is the critical index, *a* is the spatial scale of potential fluctuations, and  $V_0$  is the amplitude of potential fluctuations. According to the Shklovskii–Efros percolation theory, the current–voltage characteristics of SiO*x* are rectified in the *J* versus *F*<sup>γ</sup> coordinates.  $W_p^e$ 



**Fig. 3.** Experimental current–voltage characteristics of SiO*x* (points) measured at various temperatures and plotted in log*J* vs. *F*<sup>γ</sup> coordinates (γ = 0.52) in comparison to the results of model calculations (solid lines) for different SiO*x* compositions: (a) *x* = 1.4; (b)  $x = 1.6$ .

TECHNICAL PHYSICS LETTERS Vol. 44 No. 6 2018

The best coincidence of experiment and theory was obtained for the following sets of parameters. For  $x = 1.4$ (Fig. 3a):  $W_p^e = 0.5$  eV,  $aV_0^{0.9} = 6.69 \times 10^{-7}$  cm eV<sup>0.9</sup>, and  $J_0 = 8$  A/cm<sup>2</sup>; for  $x = 1.6$  (Fig. 3b):  $W_p^e = 0.8$  eV,  $aV_0^{0.9}$  = 7.92 × 10<sup>-7</sup> cm eV<sup>0.9</sup>, and  $J_0$  = 28 A/cm<sup>2</sup>. Then, using amplitude of potential fluctuations  $V_0 = 2.6$  eV for electrons (Fig. 2a), we obtain the following estimations of the fluctuation scale:  $a = 3.1$  nm for  $x = 1.4$  and  $a = 3.7$  nm for  $x = 1.6$ . Estimation of the specific conductivity by formula  $\sigma_0 = J_0/F$  yields  $\sigma_0 \approx 10^{-6} (\Omega \text{ cm})^{-1}$ .

According to the Shklovskii–Efros model of potential fluctuations in compensated semiconductors [8], these fluctuations have an electrostatic nature and arise due to spatial inhomogeneity of the density of ionized (charged) donors and acceptors. In the original Shklovskii–Efros model, the bandgap width in a compensated semiconductor remains constant (Fig. 2b). According to the modified model proposed in the present work, the spatial fluctuations of potential are related to fluctuations of the chemical composition of  $SiO<sub>x</sub>$  (Fig. 2a). Upon the generation of electron–hole pairs in a compensated semiconductor, the local electric field favors spatial separation of electron and hole (Fig. 2b). In SiO*x*, the local electric field favors spatial proximity of an electron and hole, with their possible subsequent recombination (Fig. 2a). Thus, SiO*x* can play the role of an effective radiative medium.

**Acknowledgments.** This study was supported in part by the Russian Science Foundation (project no. 18- 49-08001) and the Ministry of Science and Technology (Taiwan, R.O.C.) grant MOST no. 107-2923-E-009-001-MY3.

## REFERENCES

- 1. J. Kistner and M. B. Schubert, J. Appl. Phys. **114**, 193505 (2013).
- 2. S. Hernandez, P. Miska, M. Grun, S. Estrade, F. Peiro, B. Garrido, M. Vergnat, and P. Pellegrino, J. Appl. Phys. **114**, 233101 (2013).
- 3. F. Feldmann, M. Nicolai, R. Muller, C. Reichel, and M. Hermle, Energy Proc. **124**, 31 (2017).
- 4. N. V. Duy, S. Jung, K. Kim, D. N. Son, N. T. Nga, J. Cho, B. Choi, and J. Yi, J. Phys. D: Appl. Phys. **43**, 075101 (2010).
- 5. A. Mehonic, A. Vrajitoarea, S. Cueff, S. Hudziak, H. Howe, C. Labbe, R. Rizk, M. Pepper, and A. J. Kenyon, Sci. Rep. **3**, 1 (2013).
- 6. V. A. Gritsenko, Phys. Usp. **51**, 699 (2008).
- 7. J. P. Powell and M. Morad, J. Appl. Phys. **49**, 2499 (1978).
- 8. B. I. Shklovskii, Sov. Phys. Semicond. **13**, 53 (1979).
- 9. D. R. Islamov, V. A. Gritsenko, C. H. Cheng, and A. Chin, Appl. Phys. Lett. **105**, 262903 (2014).

*Translated by P. Pozdeev*